

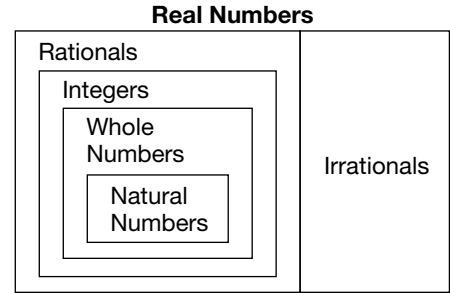
2-7 Square Roots and Real Numbers

(Pages 103–109)

If $x^2 = y$, then x is a **square root** of y . A rational number, like 81, whose square root, 9, is a rational number, is called a **perfect square**. The number 81 has two square roots, 9 and -9 . The **radical sign** $\sqrt{\quad}$ is used to indicate a nonnegative or **principal square root**. For example, $\sqrt{81} = 9$.

A square root of a positive rational number that is not a perfect square is an **irrational number**. An irrational number is a number that cannot be expressed in the form $\frac{a}{b}$, where a and b are integers and $b \neq 0$.

The set of rational numbers and the set of irrational numbers together form the set of **real numbers**. The graph of the set of all real numbers is the entire number line.



Examples

a. Find $\sqrt{0.09}$.

$$\sqrt{0.09} = 0.3 \text{ since } (0.3) \cdot (0.3) = 0.09$$

b. Find $-\sqrt{0.4}$ to the nearest hundredth using a calculator.

Practice

$$\sqrt{0.4} \approx 0.63, \text{ so } -\sqrt{0.4} \approx -0.63$$

Find each square root. Use a calculator if necessary. Round to the nearest hundredth if necessary.

1. $\sqrt{\frac{9}{16}}$ 2. $\sqrt{441}$ 3. $-\sqrt{\frac{121}{196}}$ 4. $-\sqrt{961}$ 5. $\sqrt{6.4}$

Evaluate each expression. Use a calculator if necessary. Round to the nearest hundredth if necessary.

6. \sqrt{a} , if $a = 729$ 7. $-\sqrt{cd}$, if $c = 36$ and $d = 81$ 8. $\sqrt{q+r}$, if $q = 42$ and $r = 30$

Name the set or sets of numbers to which each real number belongs. Use N for natural numbers, W for whole numbers, Z for integers, Q for rational numbers, and I for irrational numbers.

9. $\sqrt{64}$ 10. $\frac{-20}{2}$ 11. $\sqrt{50}$ 12. $-\sqrt{100}$

13. **Standardized Test Practice** A rectangular field has a length of ℓ feet and a width of w feet. The distance from any corner of the field to the diagonally-opposite corner is $\sqrt{\ell^2 + w^2}$. What is the diagonal distance across a field that is 96 feet long and 28 feet wide?

- A 144 ft B 100 ft C 124 ft D 114 ft

Answers: 1. $\frac{3}{2}$ 2. 21 3. $-\frac{11}{14}$ 4. -31 5. 2.53 6. 27 7. -54 8. 8.49 9. N, W, Z, Q 10. Z, Q 11. I 12. Z, Q 13. B