

# 4-3 Relations (Pages 205–211)

A *relation* is a set of ordered pairs. A relation can be represented by a mapping. A **mapping** shows a pairing of each  $x$  element in the *domain* with a  $y$  element in the *range*. Arrows go from the  $x$  element to the  $y$  element. You can find the **inverse** of a relation by switching the coordinates in each ordered pair.

### Example

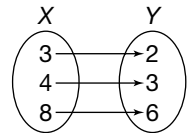
Express the relation shown in the mapping below as a set of ordered pairs. Then state the domain, range, and inverse of the relation.

set of ordered pairs:  $\{(3, 2), (4, 3), (8, 6)\}$

domain:  $\{3, 4, 8\}$  range:  $\{2, 3, 6\}$ .

To write the inverse, exchange the  $x$ - and  $y$ -coordinates.

inverse:  $\{(2, 3), (3, 4), (6, 8)\}$



### Try These Together

- State the domain, range, and inverse of  $\{(3, 7), (2, 8), (1, 9)\}$ .
- State the domain, range, and inverse of  $\{(-1, 4), (2, 4), (3, 5)\}$ .

HINT: Recall that the domain contains the first, or  $x$ -coordinates.

### Practice

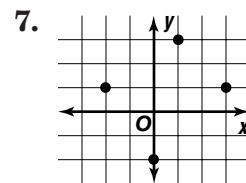
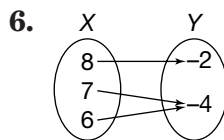
State the domain and range of each relation.

- $\{(6, 3), (9, 2), (6, 4)\}$
- $\{(10, -8), (9, -5)\}$

Express the relation shown in each table, mapping, or graph as a set of ordered pairs. Then state the domain, range, and inverse of the relation.

5.

$x$	$y$
20	15
22	18
25	19
31	20



8. **School** Emelina has noticed a ratio of 6 boys to 5 girls in her classes. She modeled this using the equation  $b = 1.2g$ , where  $b$  is the number of boys,  $g$  is the number of girls, and 1.2 is the ratio  $\frac{6}{5}$ . Explain why in this situation the solutions to this equation cannot be decimals. Use trial and error to make a table of three whole number values for  $g$  that have corresponding whole number values for  $b$ .

9. **Standardized Test Practice** What is the domain of the relation,  $\{(2, 7), (3, 5), (2, 8)\}$ ?
- A  $\{2, 3, 5, 7, 8\}$       B  $\{5, 7, 8\}$       C  $\{2, 3, 8\}$       D  $\{2, 3\}$

Answers: 1.  $D = \{1, 2, 3\}$ ,  $R = \{7, 8, 9\}$ ,  $Inv = \{(7, 3), (8, 2), (9, 1)\}$  2.  $D = \{-1, 2, 3\}$ ,  $R = \{4, 5\}$ ,  $Inv = \{(4, -1), (5, 2)\}$  3.  $D = \{6, 9\}$ ,  $R = \{2, 3, 4\}$  4.  $D = \{9, 10\}$ ,  $R = \{-8, -5\}$  5.  $\{(20, 15), (22, 18), (25, 19), (31, 20)\}$ ,  $D = \{20, 22, 25, 31\}$ ,  $R = \{15, 18, 19, 20\}$ ,  $Inv = \{(15, 20), (18, 22), (19, 25), (20, 31)\}$  6.  $\{(8, -2), (7, -4), (6, -4)\}$ ,  $D = \{6, 7, 8\}$ ,  $R = \{-4, -2\}$ ,  $Inv = \{(-4, 6), (-2, 7), (-2, 8)\}$  7.  $\{(-2, 1), (1, 3), (3, 1), (1, -1)\}$ ,  $D = \{-2, 1, 3\}$ ,  $R = \{-1, 1, 3\}$ ,  $Inv = \{(-1, 3), (1, 1), (3, -2)\}$  8. You can't have a fraction of a person. Some possible points in the table:  $\{(5, 6), (10, 12), (15, 18), (20, 24)\}$  9. D