

# 6-6 Graphing Inequalities in Two Variables

(Pages 352–357)

The solution set for an inequality in two variables contains ordered pairs whose graphs fill an area on the coordinate plane called a **half-plane**. An equation defines the **boundary** or edge of the half-plane.

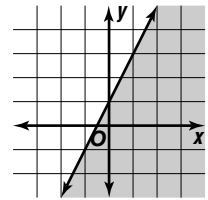
<p><b>Graphing Inequalities in Two Variables</b></p>	<ol style="list-style-type: none"> <li>1. Find the boundary by graphing the equation related to the inequality. If the inequality symbol is <math>&lt;</math> or <math>&gt;</math>, draw the boundary as a <i>dashed</i> line. If the inequality symbol is <math>\leq</math> or <math>\geq</math>, draw the boundary as a <i>solid</i> line to show that the points on the boundary are included in the solution set.</li> <li>2. Determine which of the two half-planes contains the solutions by choosing a point in each half-plane and testing its coordinates in the inequality. If the coordinates make the inequality true, shade that half-plane.</li> </ol>
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### Example

#### Graph $y - 2x \leq 1$ .

Solve the equality for  $y$ :  $y \leq 2x + 1$ . Then, graph the related equation  $y = 2x + 1$ . Draw the line as a solid line since the inequality symbol is less than or equal to. Select a point in each of the half-planes and test it in the inequality.

<p><b>Test (0, 0)</b></p> $y - 2x \leq 1$ $0 - 2(0) \leq 1$ $0 \leq 1 \text{ True}$	<p><b>Test (-1, 1)</b></p> $y - 2x \leq 1$ $1 - 2(-1) \leq 1$ $3 \leq 1 \text{ False}$
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Therefore, the half-plane that contains the point (0, 0) should be shaded.

### Practice

Find which ordered pairs from the given set are part of the solution set for each inequality.

1.  $y > 2x$ ,  $\{(-3, -7), (0, 0), (1, 3), (2, 5)\}$
2.  $3y + 2x \leq 8$ ,  $\{(-1, 5), (3, -1), (5, -1), (9, 2)\}$

Graph each inequality.

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|------------------|--------------------|----------------------|
| 3. $x > 4$       | 4. $x + y \leq 2$  | 5. $3x - 2y \leq -5$ |
| 6. $2x + 10 < 0$ | 7. $x - y \geq -4$ | 8. $y > -3$          |

9. **Jobs** It takes a librarian 1 minute to renew an old library card and 3 minutes to make a new card. Together, she can spend no more than 30 minutes renewing and making cards. Write an inequality to represent this situation, where  $x$  is the number of old cards she renews and  $y$  is the number of new cards she makes.

10. **Standardized Test Practice** Which ordered pair is a solution of  $x + 2y \leq -7$ ?  
**A** (0, 0)      **B** (8, -8)      **C** (-5, 3)      **D** (-1, 0)

Answers: 1. (1, 3), (2, 5) 2. (3, -1), (5, -1) 3-8. See Answer Key. 9.  $x + 3y \leq 30$  10. B